

Source positions of an interplanetary type III radio burst and anisotropic radio-wave scattering

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ABSTRACT

Interplanetary solar radio type III bursts provide the means for remotely studying and tracking energetic electrons propagating in the interplanetary medium. Due to the lack of direct radio source imaging, several methods have been developed to determine the source positions from space-based observations. Moreover, none of the methods consider the propagation effects of anisotropic radio-wave scattering, which would strongly distort the trajectory of radio waves, delay their arrival times, and affect their apparent characteristics. We investigate the source positions and directivity of an interplanetary type III burst simultaneously observed by Parker Solar Probe, Solar Orbiter, STEREO, and Wind and compare the results of applying the intensity fit and timing methods with ray-tracing simulations of radio-wave propagation with anisotropic density fluctuations. The simulation calculates the trajectories of the rays, their time profiles at different viewing sites, and the apparent characteristics for various density fluctuation parameters. The results indicate that the observed source positions are displaced away from the locations where emission is produced, and their deduced radial distances are larger than expected from density models. This suggests that the apparent position is affected by anisotropic radio-wave scattering, which leads to an apparent position at a larger heliocentric distance from the Sun. The methods to determine the source positions may underestimate the apparent positions if they do not consider the path of radio-wave propagation and incomplete scattering at a viewing site close to the intrinsic source position.

1. Introduction

Radio bursts at kilometer and hectometer wavelengths are generated by energetic particles propagating in interplanetary space through the plasma emission mechanism (Ginzburg & Zhelezniakov 1958; McLean & Labrum 1985; Dulk 1985; Melrose 1987). This mechanism produces fundamental and second harmonic emissions at the local plasma frequency f_{pe} and $2f_{pe}$, respectively, where $f_{pe} = \sqrt{e^2 n(r) / \pi m_e}$ is determined by the electron plasma frequency, electron number density, electron charge, and mass. The theoretical radial heliocentric distance can be calculated based on the emission frequency and assuming an interplanetary density model.

Interplanetary (IP) type III bursts provide valuable information on the electron beam trajectory, density distribution, and magnetic field configuration from the solar corona to the interplanetary medium. However, direct imaging of radio emission at kilometer and longer wavelengths is challenging, and interferometric imaging from multiple spacecraft has yet to be available. Various methods have been developed to determine the source positions of these bursts.

Direction-finding (DF) capabilities (also referred to as Goniopolarimetric (GP) capabilities) of radio receivers carried on

spacecraft can retrieve the direction, polarization, and flux of incoming electromagnetic radio waves (Fainberg et al. 1972; Reiner et al. 1998b; Cecconi & Zarka 2005; Cecconi et al. 2008; Krupar et al. 2014). Two types of DF techniques exist: spinning demodulation GP, developed for spinning spacecraft observations such as ISEE-3 and WIND/WAVES (Bougeret et al. 1995), and instantaneous GP, developed for three-axis stabilized spacecraft such as Cassini/RPWS (Gurnett et al. 2004) and STEREO/Waves (Bougeret et al. 2008) (Fainberg et al. 1972; Fainberg & Stone 1974; Manning & Fainberg 1980; Fainberg et al. 1985; Ladreiter et al. 1995; Cecconi & Zarka 2005; Cecconi et al. 2008; Martínez-Oliveros et al. 2012; Krupar et al. 2012). These antennas measure the electric field of passing electromagnetic waves, and from the DF analysis, the directions, wave flux, polarization (the four Stokes parameters), and source size of the arrival of radio waves can be determined.

For single spacecraft observation, the direction of radio waves can be determined from DF analysis, and thus the source positions can be obtained with the use of both the above directions and an interplanetary density model. For more than two spacecraft observations, the radio source is lo-

cated at the intersection of the line-of-sight directions from the direction-finding analysis of each spacecraft. It is worth noting that the accuracy of the DF results depends on the calibration accuracy of the antenna parameters, including effective electrical lengths, gains, and effective electrical vectors, which is different from assessing how accurately these electrical antenna parameters have been determined from various modeling efforts (Rucker et al. 2005; Bale et al. 2008; Reiner et al. 2009). Currently, only the DF data for STEREO can be publicly accessed. Moreover, the DF technique assumes the free propagation of radio waves and does not consider any propagation effects that may significantly affect the measured positions (Chrysaphi et al. 2018; Kontar et al. 2019).

In addition to the DF analysis, the time of arrival (ToA) difference is used to derive the trajectory of radio sources, where the centroids of the sources can be determined from two time-delay measurements from three spacecraft (Weber et al. 1977; Steinberg et al. 1984; Reiner et al. 2009; Thejappa & MacDowall 2010). Hyperbolic curves are then generated by applying relative time delays from each pair of spacecraft data to derive the source locations where the curves intersect. Another method to determine the source direction is to fit the peak intensity of the radio waves at four viewing sites, as done by Musset et al. (2021). In some cases, when Langmuir waves are observed alongside interplanetary radio bursts, the radio source can be assumed to be close to the spacecraft. In some previous studies, such as Bougeret et al. (1984), the DF method was applied to determine the emission directions of interplanetary type III storms from ISEE-3 observations, and their positions were deduced assuming the radio source region rotates rigidly with the Sun. Additionally, the source position can also be deduced by assuming the radio sources are located along the Parker spiral magnetic field line originating from the associated active region or flaring sites.

The first trajectory measurement of an interplanetary type III burst was conducted by Fainberg et al. (1972) using DF methods, where the radio waves were used to trace non-thermal electrons in the interplanetary medium. Previous studies, such as Fainberg & Stone (1974); Reiner et al. (1998a); Krupar et al. (2014), have suggested that the propagation path of electron beams is roughly along the Parker spiral magnetic field lines.

In spacecraft measurements, it is common for the heliocentric distances of interplanetary radio bursts to be larger than the distance suggested by density model. In a study by Steinberg et al. (1984), the heliocentric distances of IP type III bursts in a frequency range of 30 to 1980 kHz were found to be considerable, around 2 to 5 times the local plasma frequency. The authors suggested two possible explanations: scattering or having sources localized in overdense regions. However, their observations seemed to preclude the latter explanation. Another study by Cecconi et al. (2008) proposed that the larger heliocentric distances could be due to observing the second harmonic component, which radiates at $2f_{pe}$, or a mix of the F and H components, or strong scattering during propagation distorting the path and resulting in a longer heliocentric distance. The direction finding results of a type II burst observed by WIND/WAVES indicated that the azimuth did not intersect the isofrequency contour, suggesting heavy scattering of type II radiation in the interplanetary medium (Reiner et al. 1998b).

The inhomogeneous turbulent solar corona can strongly affect solar radio burst properties (e.g. Kontar et al. 2017; Chrysaphi et al. 2018; Kontar et al. 2019; Chen et al. 2020;

Kuznetsov et al. 2020; Musset et al. 2021; Chen et al. 2023; Clarkson et al. 2023). The propagation effects change the direction, path length, and cause a delay in the arrival times of radio waves. To understand how local density fluctuations affect the source position, we applied a ray-tracing method to simulate radio-wave propagation for anisotropic density perturbations, taking into account the effects of the Parker spiral model of the interplanetary magnetic field.

Due to the heavy reliance of direction finding analysis on complex antenna calibrations, which may produce similar results as the timing method, we apply the timing method in a relatively more straightforward way to determine the source positions from both observations and simulations. In previous studies, Weber et al. (1977) demonstrated that the burst locations determined by direction finding and time differences were in good agreement. Additionally, Reiner et al. (1998a) found that the burst profiles measured at Wind and Ulysses closely coincided after making light travel time corrections from the source to spacecraft using the known source locations from the triangulation of the direction-finding analysis of Wind and Ulysses. Moreover, Martínez Oliveros et al. (2012) showed that the source positions of type II bursts determined from both direction finding and time-of-flight analysis were consistent within the errors inherent to both techniques.

In this paper, we first apply the intensity fit and timing method to determine the source positions of an interplanetary type III burst, which has been observed by the radio instruments onboard four spacecraft: the Radio Frequency Spectrometer (RFS) on Parker Solar Probe (PSP) (Bale et al. 2016; Pulupa et al. 2017), Radio and Plasma Waves (RPW) instrument on Solar Orbiter (SolO) (Müller et al. 2020; Maksimovic et al. 2020, 2021), WAVES on Solar Terrestrial Relations Observatory (STEREO) (Bougeret et al. 2008), and the Radio and Plasma Wave Experiment (WAVES) on the WIND spacecraft (Bougeret et al. 1995). The radio emission directivity is measured from the intensity distribution at four viewing sites. Next, we derive the intensity profiles at different viewing angles corresponding to the four spacecraft from the radio-wave propagation simulations with anisotropic scattering effects. The intensity fit and timing method are also applied to determine the source positions from the simulated intensity profiles. We quantitatively investigate and compare the directivity and positions from observations of an interplanetary type III burst and from radio-wave propagation simulations.

Section 2 introduces the intensity fit and timing method and presents the source positions deduced from an IP type III burst that is simultaneously observed by four spacecraft. Section 3 shows the simulation results, including the time profiles at four viewing sites, the apparent source positions, and the source positions deduced from the intensity fit and timing method. Finally, Section 4 discusses and summarizes the main findings.

2. Observations

The interplanetary radio type III burst was observed around 09:40 UT on 05-June-2020 by four spacecraft. Time resolutions for the observations are approximately 7, 17, 35, and 60 seconds for PSP/RFS, SolO/RPW, STEREO-A/WAVES, and Wind/WAVES, respectively. The positions of the four probes are projected in the plane of the Earth's orbit in the Heliocentric Earth Ecliptic (HEE) coordinate system, as shown in the minor panel of Figure 2(b).

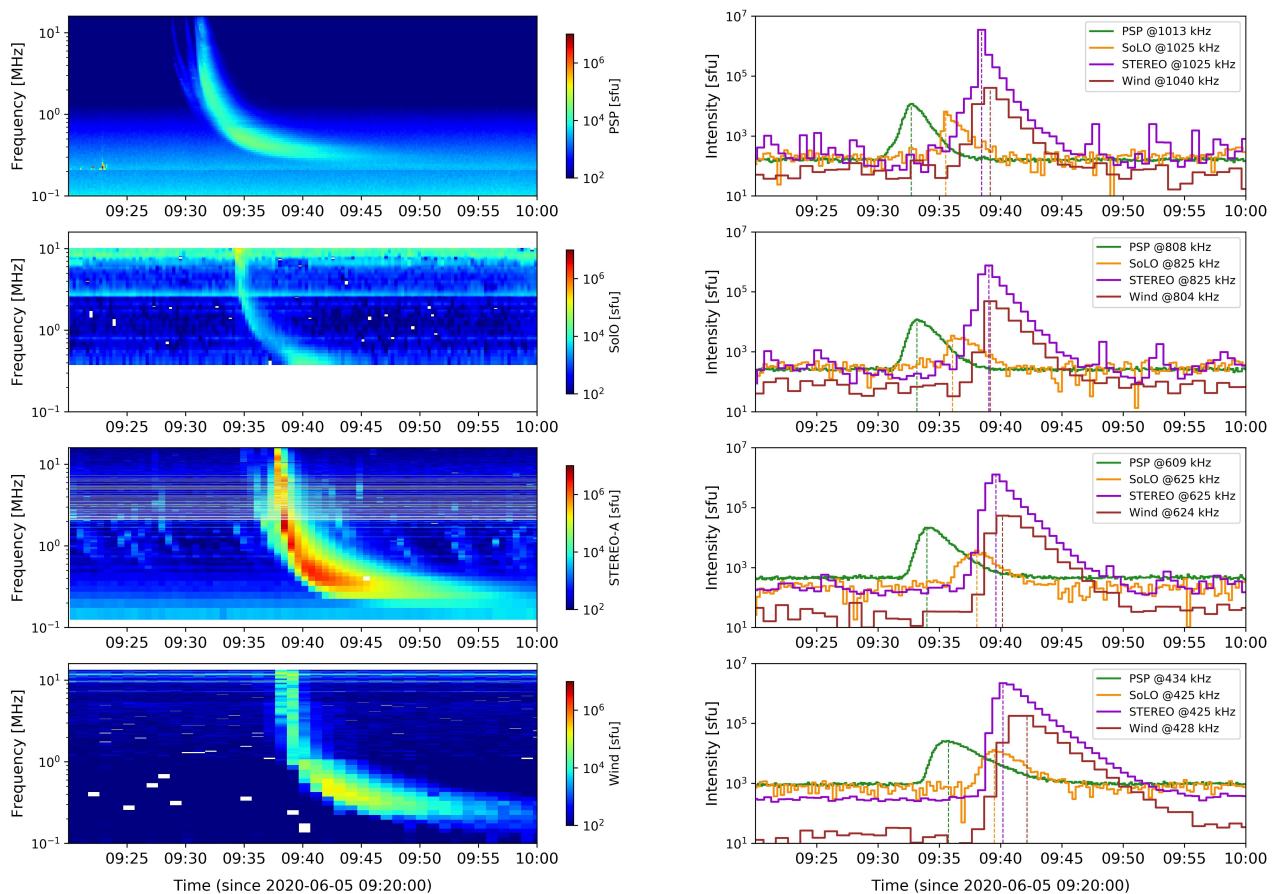


Fig. 1. Dynamic spectra (left panels) and intensity profiles (right panels) of the IP type III burst on 05 June 2020, observed by four spacecraft: PSP, SoLO, STEREO-A, and Wind. The dashed vertical lines in the right panels indicate the peak of the time profiles.

The intensities are expected to fall off with distance, approximately $1/R^2$ as the radio waves propagate away from the source. The intensities of the dynamic spectra have been corrected to 1 AU values, while no corrections are made for the different travel times of the radio waves from the source to the observers. The calibrated dynamic spectra normalized at 1 AU from ~ 200 kHz up to 16 MHz for all four instruments is shown in Figure 1 (a). We conducted the analysis between 425 kHz and 1025 kHz, as these frequencies are well observed and reliable by all four probes. The intensity curves for the four probes at frequencies close to 425 kHz, 625 kHz, 825 kHz, and 1025 kHz can be seen in Figure 1 (b). The time profiles follow a quick rise and slow decay, and the rise and decay times increase with decreasing frequency, which is consistent with previous observations of type III bursts. The time bins mark the time resolutions, and the times at peak intensities are indicated by the vertical dashed lines.

We apply the intensity fit and timing methods to determine the source position of the type III burst propagating through the interplanetary medium.

2.1. Source positions from radio emission directivity

The peak intensity of the burst at each viewing site can be described by the directivity equation for radio emissions (Bonnin et al. 2008; Bian et al. 2019; Musset et al. 2021):

$$I_i = I_0 \exp\left(\frac{\cos(\theta_i - \theta_0) - 1}{\Delta\mu}\right) \quad (1)$$

Here, θ_i denotes the longitude of probe i in the HEE coordinate system, and I_i is the peak intensity from the i probe's measurement. To obtain the maximum signal-to-noise ratio, we take the intensity at the peak of the burst. Since the frequencies for the four probes are not the same, the peak intensities from the probes are interpolated to the given frequencies. The peak intensities at the four viewing sites are fitted for each frequency using Equation 1. From this, we derive the best fits of I_0 , θ_0 , and $\Delta\mu$ from the four peak intensities (I_i , θ_i) at each viewing site, as shown in Figure 2 (a). Here, θ_0 indicates the source longitude that gives the maximal intensity, and $\Delta\mu$ represents the shape of the radio emission directivity pattern (Musset et al. 2021). The input errors of the intensity are assumed to be 50% of the peak intensity, marked as vertical lines. After applying the density model to convert the frequencies to radial distances, the source positions from the intensity fit are shown as plus signs in Figure 2 (b).

2.2. Source positions from the timing method

The technique of time of arrival assumes that delay times are caused by differences in the distances that radio waves travel from the emission region to spacecraft. By using the χ^2 method, the time delays between the spacecrafts and the radio source can be estimated. The source position can then be determined by minimizing the value of χ^2 as shown in Equation

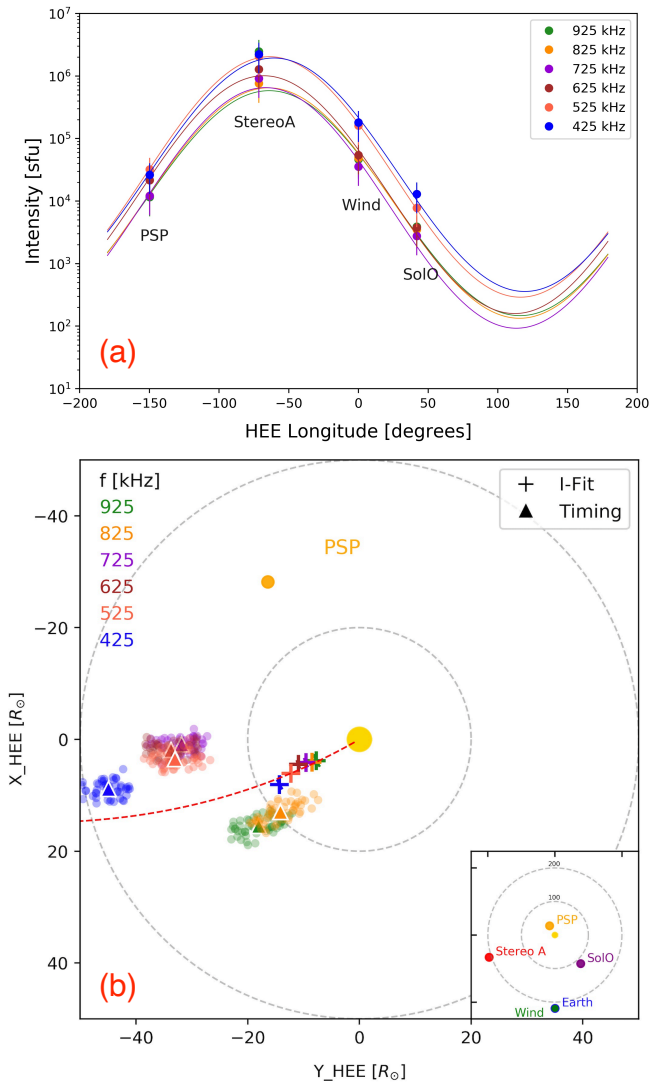


Fig. 2. Observation results. (a) Intensity fit result: The peak intensities at each frequency, corresponding to the longitudes of the four probes, are denoted by points. Vertical lines show the uncertainty, which is given to be 50% of the peak intensities. The curves represent the best-fitted intensities obtained using Equation 1. (b) Source positions: The source positions are determined using both the intensity fit (plus symbols) and timing method (triangle symbols) at six frequencies. The shadowed regions below the plus signs represent the standard deviations of errors derived from the non-linear least squares fitting of the peak intensity curves, considering 50% uncertainties of the peak intensities. The shaded dots indicate the positions determined from the timing method by sampling peak times varied by $t_i^{pk} \pm \Delta t$. The Parker spiral, with a solar wind speed of 400 km/s, is connected back to the Sun at -60 degrees and indicated as a red dashed line. In the lower right corner panel, the positions of PSP (P1), SolO (P2), STEREO-A (P3), and Wind (P4) are projected onto the plane of the Earth’s orbit in the Heliocentric Earth ecliptic (HEE) coordinate system. The dashed circles represent 100 and 200 times the solar radius.

2.

$$\chi^2 = \sum \frac{\sqrt{(x_s - x_i)^2 + (y_s - y_i)^2}/c - (t_0 - t_i^{pk})}{\Delta t_i^2} \quad (2)$$

Here, t_i^{pk} represents the peak times of the observations at a given frequency from the spacecraft i . The locations of the

probes in the ecliptic plane are denoted by x_i and y_i . We ignore the latitudes of the four spacecrafts since z_i/r_i are small on most days, roughly around ~ 0.03 , 0.01 , 0.001 , and 0.001 on 05-Jun-2020 for PSP, SolO, STEREO-A, and WIND, respectively. The radio source’s latitude is assumed to be 0, and the source is positioned in the plane of the Earth’s orbit at $(x_s, y_s, 0)$ in the HEE coordinate system. The radio waves are assumed to propagate freely at the speed of light from the source to the probes. Figure 2 (b) shows the source locations, x_s and y_s , determined using the timing method.

The deduced source position is significantly affected by the available time resolution. For instance, a time resolution of $\Delta t = 60$ s yields a distance of $c\Delta t = 25.8$ R_\odot . The uncertainties of the positions are determined using time randomization subset sampling by the peak times, generating 50 variations where the peak time is varied by $t_i^{pk} \pm \Delta t_i$. Here, Δt_i is randomly taken from a normal distribution with a mean of zero and a standard deviation of one. We obtain the average positions $(x_s, y_s, 0)$ and the errors from the average standard deviations through non-linear least squares fitting.

The radio sources at multiple frequencies are located at an average longitude of roughly -60 degrees, similar to the longitude obtained from the intensity fit method. However, the source trajectories are not easily distinguishable and range from $-47.0 \pm 11.0^\circ$ to $-88.0 \pm 4.1^\circ$, as shown in Figure 2 (b). The radial distances vary from 23.7 ± 2.0 R_\odot at 925 kHz to 46.3 ± 2.2 R_\odot at 425 kHz, which are significantly different from the distances deduced from the coronal density model. Previous observations of interplanetary type III bursts also showed larger heliocentric distances, which increase exponentially with the emission frequencies (Bougeret et al. 1984; Reiner et al. 1998a, 2009).

3. Simulations

Radio waves that propagate in the turbulent corona and interplanetary space can have their time profiles, source sizes, positions, and directivity altered by the refraction effects of large-scale density gradients and the scattering effects of small-scale density perturbations. To investigate the effects of radio wave propagation on source positions, we use a ray-tracing method to simulate radio wave propagation with anisotropic density perturbations, as developed by Kontar et al. (2019).

The simulation treats radio waves as a collection of rays with positions \mathbf{r} and wave vectors \mathbf{k} . Initially, these rays are considered to originate from a point source in the ecliptic plane, with a given heliocentric angle and distance. The emission frequency can be converted to a heliocentric distance, while the density model $n(r)$ is assumed. Here we apply the density model $n(r) = 4.8 \times 10^9 r^{-14} + 3 \times 10^8 r^{-6} + 1.39 \times 10^6 r^{-2.3}$ (r is expressed in solar radii), which is from an analytical approximation (Equation 43 in Kontar et al. (2019)) of the Parker density profile (Parker 1960). As radio waves propagate and undergo scattering in the corona, their positions and wave vectors change, and these can be determined from numerical solutions of the Fokker-Planck equation and Hamilton’s equations in an unmagnetized plasma, as described in Kontar et al. (2019). Once fully scattered, the rays arrive at a given sphere beyond which the scattering effects can be considered negligible. The arrival times, final positions, and wave vectors are recorded to produce the time profiles and images. The time profiles of the simulated radio waves after propagation can be presented by the histogram of the rays’ arrival times.

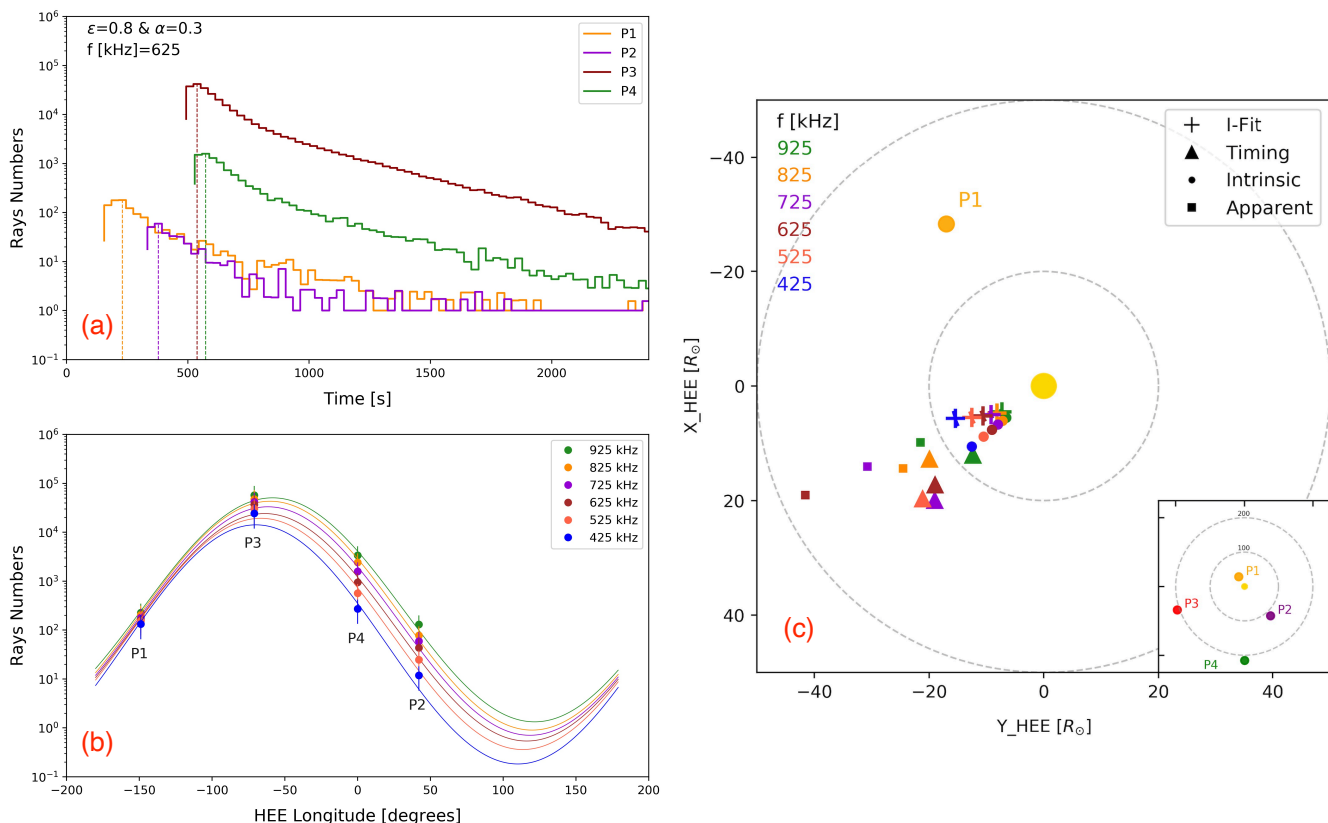


Fig. 3. Simulation results. (a) Time profiles at 625 kHz for multiple viewing angles. The collection of rays is restricted to latitudes within the range of $0.85 < \cos \phi < 1$. The times of peak intensity are marked as vertical dashed lines. (b) Intensity fit results. The four viewing longitudes are -149° (P1), 42° (P2), -71° (P3), and 0° (P4) degrees. The intensity errors are set at 50% of the peak intensities and displayed as vertical lines. (c) Positions of the intrinsic source (initial positions determined based on the density model) (solid circle symbols), the apparent source (deduced from scattering simulations) (solid square symbols), as well as source positions derived from intensity fits (plus symbols) and timing method (solid triangle symbols).

The simulated properties of the radio waves depend mainly on four factors: the frequency ratio over the local plasma frequency, the level of density fluctuations ϵ , the anisotropic parameter α , and the heliocentric angle θ_s of the intrinsic source. We consider a fundamental emission frequency of 1.1 times the local plasma frequency. Emissions that are closer to the plasma frequency undergo stronger scattering, resulting in a wider time profile with a longer duration. The level of density fluctuations ϵ is set to be 0.8, comparable to Kontar et al. (2019). It should be noted that ϵ is a relative level of density fluctuation that depends on the inner and outer scales of the density fluctuations. Stronger density fluctuations, corresponding to larger ϵ values, result in stronger scattering, later arrival times, and longer durations. The anisotropy is defined as the ratio of the perpendicular and parallel correlation lengths of the density perturbations. Anisotropic density perturbations with $\alpha = 0.2-0.3$, predominantly in the perpendicular direction to the magnetic field, are required to explain observed solar radio bursts (Kontar et al. 2019; Kuznetsov et al. 2020; Chen et al. 2020; Musset et al. 2021). When $\alpha < 1$, radio wave propagation aligns more closely with the radial direction, resulting in a narrower time profile. Stronger anisotropy, corresponding to smaller α values, can reduce the duration of the radio emissions. We use $\alpha = 0.3$ following (Kontar et al. 2019; Musset et al. 2021).

The emitted frequencies are set up to span from 425 to 925 kHz in steps of 100 kHz. The corresponding emission region is situated at a heliocentric distance ranging from 16.4 to $8.6R_{\odot}$. In our simulations, we trace 1×10^6 photons through the corona until all rays arrive at a sphere with a radius of 1 AU. Initially, the rays are located at a heliocentric angle of -50° . The resulting apparent source is located at $\sim -60^\circ$, which agrees with the average longitude of the radio source inferred from observations of the interplanetary type III burst. In order to match the positions of four probes, we collect rays at a 1 AU sphere with viewing angles of -149 , 42 , 0 , and -71 degrees for PSP (P1), SOLO (P2), STEREO-A (P3), and WIND (P4), respectively. All probes are nearly lying in the ecliptic plane, and their latitudes are ideally close to 0. To obtain a better time profile with less statistical error, we set the latitude of the collection positions to $0.85 < \cos \phi < 1$ and center the longitudes at viewing angles with a spread of 10 degrees. The rays that arrived at 1 AU with wave vector (k_x, k_y, k_z) and position (r_x, r_y, r_z) are traced back to the locations of the probes. The number of photons arriving at each viewing site varies over time, as shown in Figure 3 (a).

We fit the peak intensities at different viewing longitudes using Equation 1 (Figure 3 (b)). The uncertainty is set to 50% of the intensity, and a statistical Poisson weighting is applied to the intensity fit. The longitude (θ_0) at which the intensity reaches its maximum is regarded as the most probable direc-

tion of the source position. The heliocentric radial distance is assumed to be the same as the initial radial distance deduced from the density model for each frequency. Source positions ($r^{\text{I-fit}}$, $\theta_0^{\text{I-fit}}$) estimated from the intensity fit method are shown in Figure 3 (c). We also use the timing method to determine the source position. The times at which the peak intensity occurs are identified and fitted using Equation 2. The source positions determined from timing are marked as triangle symbols in Figure 3 (c).

The apparent source position is inferred from the image centroid and the direction of the centroid. The centroid direction corresponds to the emission directivity peak, defined as $\mu = k_z/|\mathbf{k}|$, where \mathbf{k} is the wave vector, and the z direction is the sun-earth direction.

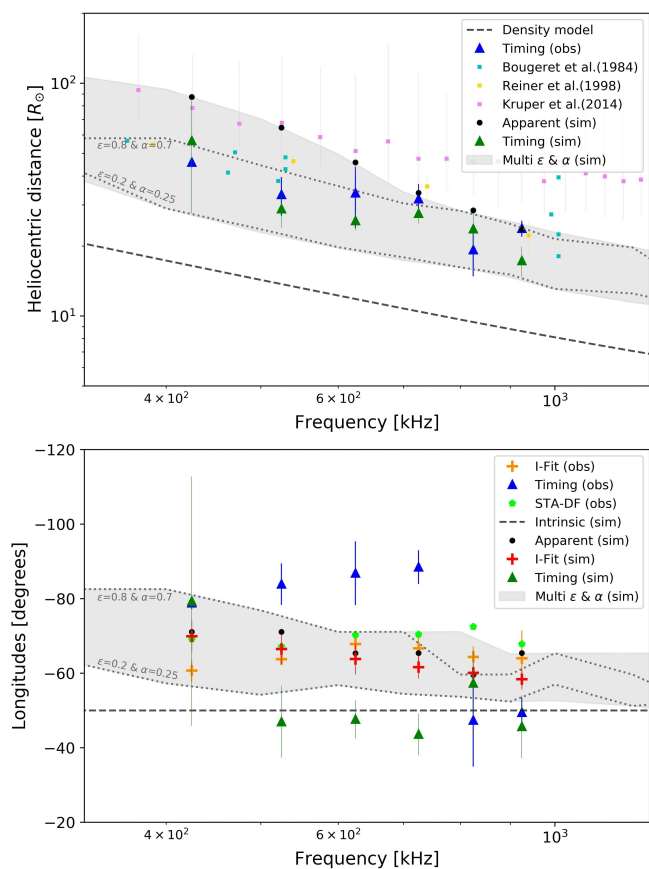


Fig. 4. Heliocentric distances (upper panel) and longitudes (lower panel) of the source are deduced from observations of four spacecraft (obs) and simulations (sim) of radio wave propagation for anisotropic scattering effects. The dashed line represents the radial distance calculated from the density model, which corresponds to the heliocentric distances of the true source. The referenced distances of the IP type III bursts from spacecraft observations are obtained from previous studies (Bougeret et al. 1984; Reiner et al. 1998a; Krupar et al. 2014). The source positions deduced from the intensity fit and timing method, based on the intensity profiles in simulations (with $\epsilon=0.8$ and $\alpha=0.3$), are depicted as red plus symbols and dark green triangle symbols, respectively. The gray shadow indicates the apparent source positions obtained from simulations considering a range of ϵ values from 0.2 to 0.8 and α values from 0.25 to 0.7. The green symbols (STA-DF) indicate the directions of this type III burst as determined by the Direction Finding (DF) measurement of STEREO-A.

4. Discussion

To determine the source positions of interplanetary type III bursts, there are various methods that can be implemented. One such method is triangulation using direction finding (DF) analysis, which requires measurements from at least two spacecraft. Another method is the timing method, which can be used when there are three or more spacecraft measurements available. In addition, it is possible to deduce the direction of the radio source from a single spacecraft DF measurement, or from the intensity fit that relies on the absolute flux from at least three spacecraft measurements. In this study, we have utilized both the intensity fit and timing method to determine the source positions of an interplanetary type III burst. This is the first time these methods have been applied to radio wave simulations with anisotropic scattering effects and compared with the measurement results.

Four space-based radio instruments, namely PSP/RFS, Solo/RPW, STEREO-A/WAVES, and WIND/WAVES, provided the four viewpoints from which the burst was detected. By exploiting the significant separation between these spacecraft, the source directions were determined through intensity fits performed on peak intensities from multiple viewing locations. The timing method relies on the arrival time difference between two spacecraft to locate the source position, assuming that the radio waves propagate in straight lines. Timing measurements are ideal for determining source locations when the spacecraft and radio source are at vastly different distances from each other, as the propagation times can exceed time resolutions.

The heliocentric distances and directions in the ecliptic plane at each frequency are shown in Figure 4. The radio source's radial trajectory was deduced from the intensity fits, while the heliocentric distances were not accessed. The radio source is found to be located further away with decreasing frequency. The heliocentric distances followed a power law function with the frequency of $r = (20.04 \pm 2.55) \times f^{-0.94 \pm 0.21}$. Our measurement is consistent with previous studies, which have also found heliocentric distances estimated from radio triangulation to be larger than the ones computed from coronal density models (Newkirk 1961; Saito et al. 1977) (eg. from Steinberg et al. 1984; Bougeret et al. 1984; Leblanc et al. 1998; Reiner et al. 2009; Krupar et al. 2014; Badman et al. 2022).

The propagation of radio waves in interplanetary space is influenced by scattering on density fluctuations, leading to changes in time profiles, directivity, and source positions. To simulate radio-wave propagation, we use the ray tracing method and predict intensity profiles at various viewing angles. The sequential arrival of rays and the relative peak intensity at multiple viewing angles show similarities to observations. In Figure 3 (c), we compare the source positions from imaging with those deduced from the intensity fit and timing method, finding that the direction deduced from the intensity fit is close to that of the apparent source, which deviates from an angle from the given intrinsic source and seems to be closely aligned with the Parker spiral magnetic field. However, the heliocentric distances and longitudes determined from the timing method do not match the apparent sources, suggesting that the source positions may be underestimated.

The time delays between two observers depend on two factors: the propagation distance from the source to the observer and the scattering time that varies as the rays travel towards distinct viewing sites. Our simulations suggest that anisotropic scattering leads to larger heliocentric distances

for the apparent position than expected from the intrinsic radio source. While the radial distances of the radio source at 525 kHz from imaging and deduced from the triangulation method show 64.6 and 35.4 R_{\odot} , the initial radial distance is 13.7 R_{\odot} from the coronal density model.

The active region 12765 is responsible for initiating this type III burst, and the PSP spacecraft is located behind it, as introduced from Stanislavsky et al. (2022). They also suggest that PSP can detect the radio emission from behind due to the radio producing electrons propagating in a dense loop. We note that the radio emissions can be detected backward due to refraction and scattering, and the directivity distribution shows that the radio emissions cover broad viewing angles and are centered around -60 degrees apart from the Sun-Earth directions. Moreover, the observed source positions are displaced away from the locations where emission is produced, suggesting that they are consistent with radio-wave propagation for anisotropic scattering, which would lead to an apparent position at a larger heliocentric distances from the Sun.

Correcting the source position from the radio-wave propagation with anisotropic scattering effects is challenging. Attempts have been made to include the effects of refraction, such as Thejappa & MacDowall (2010), but we find it is difficult to diagnose the anisotropy parameter and the relative density fluctuation level of the interplanetary turbulence from only the dynamic spectra, and scattering is event-dependent.

Many factors may affect the estimation of source positions, such as time resolutions, intensity uncertainties, frequency differences, assumptions about the radio source location, fundamental or harmonic emissions, and the intrinsic source size. We simplify the simulation by assuming a point source and not considering the actual source size, while the observed intensity profile is the result of the convolution between the intrinsic emission and broadening due to scattering (Chen et al. 2020). Additionally, each spacecraft may detect a different section of the extended source, which may have significant size or comprise multiple emitting regions. Another important factor that affects the determination of the source position is whether the radio waves experience full scattering effects during their propagation through all spacecraft. The proximity of PSP to the radio source does not guarantee full scattering effects during radio-wave propagation, and some scattering effects may still occur after passing through the spacecraft.

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